

**Abstract**

How should monetary policy respond to large fluctuations in world food prices? We study this question in an open economy model in which imported food has a larger weight in domestic consumption than abroad and international risk sharing can be imperfect. A key novelty is that the real exchange rate and the terms of trade can move in opposite directions in response to world food price shocks. This exacerbates the policy trade-off between stabilizing output prices *vis a vis* the real exchange rate, to an extent that depends on risk sharing and the price elasticity of exports. We characterize implications for dynamics, optimal monetary policy, and the relative performance of practical monetary rules. While CPI targeting and expected CPI targeting can dominate PPI targeting if international risk sharing is perfect, even seemingly mild departures from the latter make PPI targeting a winner.

*Keywords:* Monetary Policy, Small Open Economy, Real Exchange Rates, Terms of Trade

*JEL classification:* F4,E5

**1. Introduction**

Inflationary bursts worldwide have been long associated with spiralling food prices. Granger-causality tests on post-1970 data corroborate this old-standing regularity, as global food commodity prices tend to lead rather than lag global CPI changes.<sup>1</sup> That food price shocks greatly matter for aggregate inflation has become particularly important to many inflation targeting countries over the past decade: a burst of food commodities inflation in 2007-08 led to widespread overshooting of inflation targets; this was followed by considerable undershooting of the targets once food prices receded. This evidence may not seem surprising, since food weighs heavily in most consumption baskets and is not easily substitutable by other goods. The surprise is that the monetary policy literature has given little attention to its implications.

To help filling the gap, this paper addresses the related questions of how far monetary policy should accommodate food price shocks and which policy rules, among those that are practically implementable, are best suited to shore up welfare. We model a small open economy that is a net food importer and where food weighs more heavily in domestic consumption than in world consumption. Faced with unexpectedly high world food prices, this economy experiences a terms of trade deterioration, higher CPI inflation, and a real exchange rate appreciation. This combination poses particularly stark policy trade-offs between domestic and external stabilization objectives. We characterize the transmission dynamics of exogenous shocks underlying these trade-offs under various degrees of international financial integration, and examine the implications for welfare and monetary policy choices.

In doing so, this paper relates to a rapidly growing literature on monetary policy in open economies, usefully surveyed by Corsetti, Dedola, and Leduc (2010). As emphasized by these authors, recent dynamic New Keynesian open economy models can yield different monetary policy prescriptions from their closed economy counterparts. In the latter, as summarized by Woodford (2003) and Gali (2008), optimal monetary policy is typically geared towards replicating a flexible price or natural outcome, suitably attainable through the stabilization of producer prices. Further, in the absence of mark-up/cost-push shocks and/or real wage rigidities, these models also imply that PPI stabilization is conducive to output stabilization. In contrast, consumption and production openness introduce additional policy trade-offs. In particular, small open economies can gain from steering the real exchange rate and the terms of trade. This "terms of trade externality" (Corsetti and Pesenti 2001) implies that the flexible price equilibrium is not generally optimal, hence raising the question of whether PPI stabilization remains the best policy. Several studies of the model developed by Gali and Monacelli (2005) have provided a basically affirmative answer (e.g. Faia and Monacelli 2008, and Di Paoli 2009). However, these studies have placed severe restrictions on the model environment, especially perfect international risk sharing.

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<sup>1</sup>This is so even after controlling for oil prices. These claims readily follow from regressing changes in the GDP weighed world CPI on changes in the log of the IMF price indices of global food and of oil commodities over the period 1970-2011. The F-statistic on the exclusion of lagged food inflation is significant at 1%. In contrast, the significance of Granger-causality F-statistics on oil prices is generally weaker and of varying significance across sub-periods.

This paper extends the environment of these previous studies in several ways. We model "food" as a key import, traded in flex-price competitive markets, and which enters as a distinct commodity in the home consumption basket with possibly a very low elasticity of substitution *vis a vis* other goods. Other extensions include: (i) global food prices can vary widely relative to the world price index; (ii) food expenditure shares at home and the rest of the world can differ significantly; (iii) the export price elasticity of the world demand for home exports can differ from the intratemporal elasticity of substitution of home and imported goods in consumption; (iv) international risk sharing can be incomplete.

Extensions i and ii allow our model to capture a much overlooked empirical regularity, already mentioned but still worth emphasizing: with shocks to the world relative price of food, the terms of trade and the real exchange rate can move in opposite directions. Such a negative covariance is ruled out by previous models. Empirically however, and as shown in Figure 1, a negative covariance is often found in economies that are net food importers and that export sticky price high elasticity goods (as allowed by extension iii). Extension iv, that international risk sharing can be imperfect, hardly needs justification. But departing from the assumption of perfect risk sharing introduces several technical difficulties, which may explain why the assumption is ubiquitous. In this paper we follow Schulhofer-Wohl (2011) in assuming complete financial markets but also a costly wedge in the transferring of resources in and out of the domestic household. This formulation implies that domestic consumption is a combination of the polar cases of perfect risk sharing and portfolio autarky, leading to a specification that is parsimonious, intuitive, and relatively easy to calibrate. As such, it is of independent interest.

[PLEASE INSERT FIGURE 1 APPROXIMATELY HERE]

In the resulting setting, we provide a complete characterization of Ramsey and natural allocations, as well as of optimal feasible optimal policy, extending the analysis of Faia and Monacelli (2008) and Di Paoli (2009). We combine both analytical approaches with extensive numerical calibrations to flesh out the role of the degree of international risk sharing and of structural elasticities for optimal policy and welfare-based comparisons of policy rules.

Main findings include: First, in the presence of shocks to world food prices, the relative desirability of home inflation versus output gap stabilization varies significantly depending on the extent of risk sharing and on the export price elasticity. In particular, if the latter is sufficiently but also realistically high (that is, as the economy is "smaller" in export markets), less international risk sharing implies that optimal policy places a heavier weight on domestic price stabilization. Second, when the variance of imported food price shocks is calibrated to be as large as in the data, international risk sharing is perfect, and the home economy's export price elasticity is not too low, CPI targeting can deliver higher welfare than PPI targeting. But targeting "expected" or forecast CPI is even superior. The reason is that expected CPI targeting exploits more heavily the terms of trade externality, resulting in more stable real exchange rate and consumption; in doing so, it delivers a better approximation to the optimal allocation than the competing rules. Third, the welfare-superiority of PPI targeting is easily restored if international risk sharing is less than complete: for a wide range of the other parameters, even small values of the financial transfer cost wedge imply that PPI dominates other rules. In this sense, the conditions for PPI stabilization to be the optimal policy are broader than highlighted in previous work, which relied on perfect risk sharing and the domestic good substitution elasticity being the same as the export good elasticity. Fourth, an optimal feasible policy can be characterized by a "flexible targeting rule", a linear combination of domestic inflation and deviations of output from a target. The output target is a function of exogenous shocks, with coefficients that depend on elasticities of demand and the degree of risk sharing.

The remainder of the paper proceeds as follows. Section 2 lays out the basic framework. Section 3 discusses the model's linearized representation and dynamic responses to world food price shocks. Section 3 characterizes optimal policy. Numerical calibrations and welfare ranking of policy rules is presented in section 4. Section 5 concludes. To preserve space, a Technical Appendix (available from ScienceDirect) gathers several formal expressions and derivations.

## 2. Model

We study a small open economy populated by identical agents that consume a domestic good and imported food. The domestic good is an aggregate of intermediate varieties produced with domestic labor. The intermediates sector is characterized by monopolistic competition and nominal price rigidities.

The share of food is larger in the domestic consumption basket than in the world basket, so PPP does not hold. Further, the world price of food in terms of world consumption is exogenous. One consequence is that the real exchange rate appreciates when the world relative price of food rises, and domestic consumption fluctuates with world food prices. Also, and in contrast with previous work, our model implies that the terms of trade and the real exchange rate can move in opposite directions.

Another novelty is that international risk sharing is allowed to be imperfect because domestic households may face costs of transferring resources, as in Schulhofer-Wohl (2011).

## 1 2.1. Households

2 The economy has a representative household that maximizes the expected value of  $\sum_{t=0}^{\infty} \beta^t \left[ \frac{C_t^{1-\sigma}}{(1-\sigma)} - \varsigma \int_0^1 \frac{N_t(j)^{1+\varphi}}{1+\varphi} dj \right]$ ,  
 3 where  $0 < \beta < 1$ ,  $\sigma, \varphi$ , and  $\varsigma$  are parameters,  $C_t$  denotes consumption, and  $N_t(j)$  is the supply of labor employed by  
 4 a firm belonging to industry  $j \in [0, 1]$ . As in Woodford (2003), there is a continuum of industries, each employing a  
 5 different type of labor. Labor types are imperfect substitutes if  $\varphi > 0$ .

Consumption is a C.E.S. aggregate of a home final good  $C_h$  and imported food  $C_f$  :

$$C_t = \left[ (1-\alpha)^{1/\eta} C_{ht}^{(\eta-1)/\eta} + \alpha^{1/\eta} C_{ft}^{(\eta-1)/\eta} \right]^{\eta/(\eta-1)}$$

where  $\eta$  is the elasticity of substitution between home and foreign goods, and  $\alpha$  is a parameter that measures the degree of openness. The associated price index, or CPI, expressed in domestic currency, is then

$$P_t = \left[ (1-\alpha) P_{ht}^{1-\eta} + \alpha P_{ft}^{1-\eta} \right]^{1/(1-\eta)} \quad (1)$$

where  $P_{ht}$  and  $P_{ft}$  are the domestic currency prices of the home good and imports. Also, given total consumption  $C_t$  and prices  $P_{ht}$  and  $P_{ft}$ , optimal demands for home goods and foreign goods are given by

$$C_{ht} = (1-\alpha) (P_{ht}/P_t)^{-\eta} C_t \quad (2)$$

6 and  $C_{ft} = \alpha \left( \frac{P_{ft}}{P_t} \right)^{-\eta} C_t$ , where  $P_{ht}/P_t$  is the price of home output in terms of home consumption (the "real" price of  
 7 home output).<sup>2</sup>

The household owns domestic firms and receives their profits. It chooses consumption and labor effort taking prices and wages as given. With respect to trade in assets, we depart from Gali and Monacelli (2005), Di Paoli (2009) and others in allowing for financial frictions and imperfect risk sharing across countries. Specifically, we borrow Schulhofer-Wohl's (2011) closed-economy assumption that the typical household incurs deadweight costs if it transfers resources in or out of the household. Denoting the household's current nonfinancial income by  $H_t$ , the assumption is that the household has to pay an extra cost of  $\varpi \Phi(C_t, H_t)$  units of consumption, where  $\Phi(C, H) = \frac{\varsigma}{2} \left( \log \left( \frac{C}{H} \right) \right)^2$  and  $\varpi$  is a parameter controlling the severity of this friction. This formulation implies that optimal risk sharing is given by

$$C_t^\sigma [1 + \varpi \Phi_{Ct}] = \kappa X_t (C_t^*)^\sigma \quad (3)$$

8 where  $\kappa$  is a positive constant,  $C_t^*$  is an index of world consumption,  $X_t$  is the *real exchange rate* (the ratio of the price  
 9 of world consumption to the domestic CPI, both measured in a common currency), and  $\Phi_{Ct} = \Phi_C(C_t, H_t)$  is the partial  
 10 derivative of  $\Phi$  with respect to  $C$  evaluated at  $(C_t, H_t)$ .<sup>3</sup> If  $\varpi = 0$ , the preceding expression reduces to the usual  
 11 perfect international risk sharing condition: marginal utilities of consumption at home and abroad are proportional up  
 12 a real exchange rate correction. For nonzero  $\varpi$ , optimal risk sharing takes into account that each consumption unit  
 13 transferred to domestic households involves the extra transfer cost  $\varpi \Phi_c$ , explaining the appearance of this term in the  
 14 left hand side. Financial autarky corresponds to  $\varpi$  going to infinity: in that case, and using  $Y_t$  to denote domestic  
 15 output,  $C_t = H_t = (P_{ht}/P_t) Y_t$  in equilibrium, so the trade balance is zero in all periods. Schulhofer-Wohl's assumptions  
 16 thus capture market incompleteness in a way that is attractive in its simplicity, encompassing perfect risk sharing and  
 17 portfolio autarky as special cases, and (as found below) retaining tractability.<sup>4</sup>

Next, if  $W_t(j)$  is the domestic wage for labor of type  $j$ , optimal labor supply is given by the equality of the marginal

<sup>2</sup>Home bias corresponds to the case  $\alpha < 1/2$ . We have assumed  $\eta \neq 1$ . If  $\eta = 1$ ,  $C_t$  and  $P_t$  are Cobb Douglas.

<sup>3</sup>Let  $\Omega_{t,t+1}$  denote the domestic currency price at  $t$  of a security that pays a unit of domestic currency at  $t+1$  conditional on some state of nature  $s'$  being realized at that time. Then optimal consumption requires  $\Omega_{t,t+1} = \beta \frac{P_t}{P_{t+1}} \left( \frac{C_{t+1}}{C_t} \right)^{-\sigma} \frac{1 + \varpi \Phi_c(C_t, H_t)}{1 + \varpi \Phi_c(C_{t+1}, H_{t+1})}$ , reflecting that the effective cost of an extra unit of consumption at  $t$  is not  $P_t$  but  $P_t(1 + \varpi \Phi_c(C_t, H_t))$ . For the rest of the world, we assume that there is no transferring cost, so the corresponding FOC is  $\Omega_{t,t+1} = \beta \frac{S_t P_t^*}{S_{t+1} P_{t+1}^*} \left( \frac{C_{t+1}^*}{C_t^*} \right)^{-\sigma}$ . The usual derivation for the complete markets case can then be amended to yield (3).

<sup>4</sup>One might, of course, object that  $\varpi$  may be time-varying and not readily mapped onto observables. But similar objections could be equally raised to the obvious alternative, which is a bond economy. As noted in Schulhofer-Wohl (2011), assuming risk is shared imperfectly via noncontingent bond contracts also amounts to a reduced form specification. In practice, risk sharing takes place through a variety of other financial instruments, both formal and informal, official and private.

disutility of labor with the marginal utility of the real wage, corrected by marginal transfer costs:

$$\varsigma C_t^\sigma N(j)_t^\varphi = \frac{W_t(j)[1 - \varpi\Phi_{Ht}]}{P_t [1 + \varpi\Phi_{Ct}]} \quad (4)$$

Finally, the domestic safe interest rate is given by

$$\frac{1}{1 + i_t} = \beta E_t \left[ \left( \frac{C_{t+1}}{C_t} \right)^{-\sigma} \frac{P_t (1 + \varpi\Phi_{Ct})}{P_{t+1} (1 + \varpi\Phi_{C_{t+1}})} \right] \equiv E_t M_{t,t+1} \quad (5)$$

1 where we have defined  $M_{t,t+j}$  as the period  $t$  pricing kernel applicable to nominal payoffs in period  $t + j$ . This extends  
2 the familiar expression of the frictionless asset trade case.

### 3 2.2. Prices

4 For simplicity, we assume that all food is imported and that the world price of food is exogenously given in terms of  
5 a world currency. Using asterisks to denote prices denominated in world currency, the domestic currency price of food  
6 is then  $P_{ft} = S_t P_{ft}^*$ , where  $S_t$  is the nominal exchange rate (domestic currency per unit of foreign currency). So, there  
7 is full pass through from world to domestic food prices.

8 Likewise, we assume that the world currency price of the world consumption index is exogenous.<sup>5</sup> Denoting it by  $P_t^*$ ,  
9 the real exchange rate is then  $X_t = S_t P_t^*/P_t$ . It is useful also to define the *terms of trade* by  $Q_t = P_{ft}/P_{ht} = S_t P_{ft}^*/P_{ht}$ .

As in other models, the terms of trade and the real price of home output are essentially the same, since (1) implies  
that  $(P_{ht}/P_t)^{-(1-\eta)} = (1-\alpha) + \alpha Q_t^{1-\eta}$ . But, in contrast with those other models, the real exchange rate and the terms  
of trade are not proportional to each other, reflecting fluctuations in the world price of food relative to the world CPI.  
The previous definitions imply the following relation between the real exchange rate and the real price of home output:

$$P_{ht}/P_t = \left[ \frac{1 - \alpha X_t^{1-\eta} Z_t^{1-\eta}}{1 - \alpha} \right]^{1/(1-\eta)} \quad (6)$$

10 where  $Z_t = P_{ft}^*/P_t^*$  is the *world's relative price of food*, which we take as exogenous.

11 An improvement in the terms of trade (a fall in  $Q_t$ ) implies an increase in the real price of output ( $P_{ht}/P_t$ ). If  $Z_t$  is  
12 held fixed, (6) then implies that  $X_t$  must fall (a real appreciation). But this logic does not apply when  $Z_t$  moves:  $X_t$   
13 and  $Q_t$  can then move in opposite directions.

14 Since this aspect of our model is relatively novel, it deserves further elaboration. Other models have typically assumed  
15 that home agents consume a domestic aggregate and a foreign aggregate (such as  $C^*$  in our model), and that there  
16 is some home bias, so that PPP does not hold. In contrast, we assume that home agents do not consume the foreign  
17 aggregate but instead a different good (food). This would not make a difference if the relative price of food were fixed  
18 in terms of the foreign aggregate (e.g. if  $Z$  were constant). So the main differences between our model and previous  
19 ones emerge because  $Z$  is allowed to fluctuate.

20 In particular, the standard specification implies, as just discussed, a very tight link between the terms of trade and  
21 the real exchange rate: with constant  $Z$ ,  $X_t$  and  $Q_t$  must *always* move in the same direction. Using hatted lowercase  
22 variables for log deviations of variables from steady state, it turns out that  $\hat{x}_t = (1-\alpha)\hat{q}_t$  to a first order approximation,  
23 so that (to second order)  $Var(\hat{x}_t) = (1-\alpha)^2 Var(\hat{q}_t)$ : if  $\alpha < 1$ , the variance of the real exchange rate is proportional to  
24 and strictly less than the variance of the terms of trade. These implications seem quite restrictive.

25 In our model, in contrast,  $\hat{x}_t = (1-\alpha)\hat{q}_t - \hat{z}_t$  to first order. We then see that fluctuations in the relative price of food  
26 mean that  $\hat{x}_t$  and  $\hat{q}_t$  can move in opposite directions (in response of shocks to  $\hat{z}_t$ ). This is more likely to be the case if  
27 the economy is very open (i.e. if  $\alpha$  is large) or if food prices are very volatile (i.e. if the typical size of  $\hat{z}_t$  is large). We  
28 also see that the variance of  $\hat{x}$  can be larger than the variance of  $\hat{q}$ , depending on the volatility of  $\hat{z}$ .

29 As we will see, the volatility of food prices is also a crucial factor in the analysis of monetary policy rules. So this  
30 model suggests that a negative correlation between the real exchange rate and the terms of trade goes hand in hand  
31 with drastic changes in policy evaluation. This is natural in our model, as both aspects of the analysis reflect the impact  
32 of food price shocks.

<sup>5</sup>When calibrating the model, we make the stronger assumption that shocks to  $C^*$  and  $Z$  are independent. To justify this, one can assume that food has a negligible share in the world consumer basket, in contrast with the domestic basket. This is a defensible assumption since the share of food in the CPI is substantially higher in small emerging economies than in advanced countries.

2.3. Domestic Production

Domestic production follows Gali and Monacelli (2005), Gali (2008) and others, so we refer to those sources for brevity. The home final good  $Y_t$  is a Dixit-Stiglitz aggregate of intermediate goods varieties. Cost minimization then implies that the demand for each variety  $j \in [0, 1]$  is given by  $Y_t(j) = \left(\frac{P_t(j)}{P_{ht}}\right)^{-\varepsilon} Y_t$ , where  $\varepsilon$  is the elasticity of substitution between domestic varieties,  $P_t(j)$  is the price of variety  $j$  and  $P_{ht}$  is the relevant price index (the PPI). Each variety  $j$  is produced with only labor of type  $j$  according to the production function  $Y_t(j) = A_t N_t(j)$ , where  $N_t(j)$  is the input of type  $j$  labor and  $A_t$  is a productivity shock, common to all firms in the economy.

Firms take wages as given. We allow for the existence of a subsidy to employment at constant rate  $v$ . Hence nominal marginal cost is given by  $\Psi_{jt} = (1 - v)W_t(j)/A_t$ , where  $W_t(j)$  is the wage rate for type  $j$  labor.

Variety producers are monopolistic competitors and set prices in domestic currency following a Calvo protocol: each individual producer is allowed to change nominal prices with probability  $(1 - \theta)$ . All producers with the opportunity to reset prices in period  $t$  choose the same price, say  $\bar{P}_t$ , reflecting desired current and future markups over marginal costs (see Gali 2008 for a discussion). The price of the home final good is then given by  $P_{ht} = \left[(1 - \theta)\bar{P}_t^{1-\varepsilon} + \theta P_{h,t-1}^{1-\varepsilon}\right]^{1/(1-\varepsilon)}$ .

2.4. Market Clearing

We assume that the foreign demand for the domestic aggregate is given by a function of its price relative to  $P_t^*$  and the index  $C_t^*$  of world consumption. Hence market clearing for the home aggregate requires:

$$Y_t = (1 - \alpha) (P_{ht}/P_t)^{-\eta} [C_t + \varpi \Phi(C_t, (P_{ht}/P_t) Y_t)] + \varkappa \left(\frac{P_{ht}}{S_t P_t^*}\right)^{-\gamma} C_t^* \tag{7}$$

where  $\varkappa$  is a constant and  $\gamma$  is the price elasticity of the foreign demand for home exports, which is allowed to differ from the domestic elasticity for the home goods,  $\eta$ . The first term in the right hand side is the domestic demand, inclusive of financial transfer costs, for the domestic aggregate; it uses the fact that, in equilibrium, nonfinancial household income equals the value of domestic production, that is,  $H_t = (P_{ht}/P_t) Y_{ht}$ .

Once a rule for monetary policy is specified, the model can be solved for the equilibrium home output, consumption, and relative prices. We discuss implications in turn.

3. Linear Approximation and Implications

A log linear approximation of the model around its nonstochastic steady state is described in Table 1. As mentioned, we use hatted lowercase variables to denote log deviations from steady state. Equation (L1) is the approximation of the risk sharing condition (3), with  $\psi = \sigma/(\varpi + \sigma)$  indicating the degree of risk sharing ( $\psi = 1$  denotes perfect risk sharing and  $\psi = 0$  portfolio autarky). Equations (L2) and (L3) are linearized versions of (6) and (7). Finally, (L4) summarizes linear versions of Calvo pricing equations: it is the now familiar Phillips Curve relationship between PPI inflation ( $\pi_{ht} = \log P_{ht} - \log P_{ht-1}$ ), its expected future value, and marginal costs (the term in brackets).

[PLEASE INSERT TABLE 1 HERE]

Table 1 also displays the corresponding equations under flexible prices, whose solutions yield the "natural" values, identified by an  $n$  superscript. The natural values are linear transformations of the exogenous shocks. Finally, the table shows the equation system in terms of "gaps" or log deviations from natural values, identified with tildes.

The equations in Table 1 yield the solution of the model, up to a linear approximation, once monetary policy is specified. They also allow us to identify how conventional analysis can be modified to accommodate the particular features of our specification.

3.1. Aggregate Supply and Demand

Key to the model's transmission mechanism is the relationship between the output gap and international relative prices, as summarized by the terms of trade  $q_t$  or the real exchange rate  $x_t$ . Inserting (G1) and (G2) into (G3) yields:

$$\tilde{x}_t = (1 - \alpha)\tilde{q} = \Theta\tilde{y}_t \tag{8}$$

where

$$\Theta = \frac{(1 - \alpha)[1 - \omega(1 - \psi)]}{\omega[\alpha(\eta - \psi/\sigma) - (\gamma - \psi/\sigma)] + \alpha\omega(1 - \psi) + \gamma} \tag{9}$$

1 and  $\omega$  is the steady state ratio of domestic expenditure on home goods to home output. To interpret, consider the  
 2 case of perfect risk sharing ( $\psi = 1$ ) and of equal price elasticities of demand at home and abroad,  $\eta = \gamma$ . Then  
 3  $\Theta = (1 - \alpha)/[\eta - \omega(1 - \alpha)(\eta - 1/\sigma)]$ ; if, further,  $\eta = 1/\sigma = 1$ , as emphasized in the literature,  $\Theta = (1 - \alpha)$ . These  
 4 expressions resemble those studied in previous work, especially in highlighting the importance of the difference between  
 5  $\eta$  and  $1/\sigma$  for the output response to international relative price shocks (as discussed by Corsetti et al. 2010 and others).

6 Our derivation of  $\Theta$  in (9) extends the previous intuition in two directions: it highlights that frictions to full risk  
 7 sharing ( $\psi < 1$ ) introduce a wedge in the "gap" between  $\eta$  and  $1/\sigma$ ; and it shows that the home response of output to  
 8 relative prices changes change with the export elasticity  $\gamma$ .

Using (8) and combining (G1)-(G4) one then obtains a New Keynesian Phillips Curve:

$$\pi_{ht} = \chi \tilde{y}_t + \beta E_t \pi_{ht+1},$$

with slope

$$\chi = \lambda \left[ \varphi + \left( \psi + \frac{\alpha}{1 - \alpha} \right) \Theta + \sigma(1 - \psi) \left( 1 - \frac{\alpha}{1 - \alpha} \Theta \right) \right]$$

9 While the form of the resulting Phillips Curve is standard, our analysis shows that its slope depends on the degree  
 10 of international capital mobility (as parameterized by  $\varpi$ , which affects  $\chi$  both directly and through  $\Theta$ ), as well as on  
 11 the elasticities  $\eta$  and  $\gamma$  (which affect  $\Theta$  and hence  $\chi$ ). Food price shocks, in turn, affect natural output and hence the  
 12 output gap  $\tilde{y}$ , as implied by the equations in Table 1.

13 The aggregate demand side can be summarized by a dynamic IS curve: log linearizing the Euler equation and noting  
 14 that the definition of the CPI implies that  $\Delta p_{ht} = \log(P_{ht}/P_{ht-1}) - \log(P_t/P_{t-1}) = \pi_{ht} - \pi_t = -\frac{\alpha}{1-\alpha} \Delta(\hat{x}_t + \hat{z}_t^*)$ , one  
 15 obtains:

$$\tilde{y}_t = -\Lambda [i_t - E_t \pi_{ht+1} - r_t^n] + E_t \tilde{y}_{t+1} \quad (10)$$

where  $\Lambda = \frac{1-\alpha}{\Theta}$ , and the natural interest rate is:

$$r_t^n = E_t \left[ \sigma \Delta \hat{c}_{t+1}^* + \frac{1}{1-\alpha} (\alpha \Delta \hat{z}_{t+1} + \Delta x_{t+1}^n) \right] = E_t [\sigma \Delta \hat{c}_{t+1}^* + \Delta q_{t+1}^n - \Delta \hat{z}_{t+1}] \quad (11)$$

16 the last step having made use of  $x_t^n = (1 - \alpha)q_t^n - z_t$ .

17 Two features of the resulting IS curve are worth highlighting. One is that financial market frictions affect the  
 18 coefficient  $\Lambda$ , which depends on  $\Theta$  and hence on the market incompleteness parameter  $\psi$ . The other is that shocks  
 19 to food prices affect output through the real natural interest rate – in particular, the latter will change with expected  
 20 changes in the natural terms of trade ( $q_t^n$ ) and in the world terms of trade  $z_t$ .

### 21 3.2. Impulse Responses

22 To shed light on the dynamic responses of this economy to world food price shocks, abstract from other shocks by  
 23 setting  $\hat{c}_t^* = a_t = 0$ , and assume that  $\hat{z}_t$  follows an AR(1) process with persistence parameter  $|\rho_z| < 1$ .

For concreteness, here we assume a standard Taylor rule on PPI inflation<sup>6</sup>:

$$i_t = \phi_y \tilde{y}_t + \phi_\pi \pi_{ht} \quad (12)$$

This rule, together with the Phillips Curve and the dynamic IS curve, can then be solved for the output gap, domestic  
 inflation, and the interest rate as functions of the natural interest rate. In particular<sup>7</sup>,  $\pi_{ht} = \chi \Lambda_v r_t^n$  and  $\tilde{y}_t = (1 - \beta \rho_z) \Lambda_v r_t^n$ , where

$$\Lambda_v = \frac{1}{\left[ \frac{1-\rho_z}{\Lambda} + \phi_y \right] (1 - \beta \rho_z) + \chi (\phi_\pi - 1)}$$

24 Here we have used the fact that the natural interest rate can be written as a linear function of the food price shock:  
 25  $r_t^n = \phi E_t \Delta \hat{z}_{t+1} = -\phi(1 - \rho_z) \hat{z}_t$  for a constant  $\phi$  described below, so that  $r_t^n$  has the same autocorrelation  $\rho_z$  as  $z$ . The

<sup>6</sup>To keep the notation compact, we omit the constant in the policy rule (which equals the real interest rate in steady state). This is consistent with assuming zero inflation and zero world interest rate in steady state. Since we are abstracting from other than food price shocks, we also abstract from stochastic shocks to policy.

<sup>7</sup>This is a straightforward exercise in undetermined coefficients. See e.g. Gali (2008), subsection 3.4.1.

1 same observation allows us to rewrite the solutions for inflation and the output gap as functions of  $z_t$  :

$$\begin{aligned}\pi_{ht} &= -\chi\Lambda_v\phi(1-\rho_z)\hat{z}_t \\ \tilde{y}_t &= -(1-\beta\rho_z)\Lambda_v\phi(1-\rho_z)\hat{z}_t\end{aligned}\tag{13}$$

2 This is a closed form solution that fully characterizes the responses of the model to food price shocks. Notably, since  
3  $\chi > 0$ , home inflation and the output gap will always move in the same direction in response to  $z_t$ . This can be up or  
4 down, however, depending on elasticities. To establish the direction and respective magnitudes, we need to compute  $\phi$ ,  
5 that is, how the natural rate of interest responds to  $z$ . From the natural system of equations one obtains:

$$\phi = -\frac{\alpha\{(\sigma-1)(1-\psi)+\omega\tau\}}{\alpha\{(\sigma-1)(1-\psi)+\omega\tau\}-\gamma(1-\omega)(\varphi+\sigma(1-\psi))-\psi(1+\omega\varphi/\sigma)}$$

where

$$\tau = [(1-\psi)(\varphi+1-\eta\sigma)-\varphi(\eta-\psi/\sigma)]$$

6 This shows that  $\phi$  can be positive or negative depending on parameter values. But the expression is complex and  
7 difficult to interpret directly. We can gain intuition, however, by examining the extremes of perfect risk sharing and  
8 portfolio autarky. Given (L1), any intermediate case is a convex combination of those two.

9 With perfect risk sharing:  $\psi = 1$  and  $\phi$  simplifies greatly:

$$\phi = \frac{-\alpha\omega\varphi(\eta-1/\sigma)}{1+\varphi[(1-\omega)\gamma+\omega(\frac{1-\alpha}{\sigma}+\alpha\eta)]} \quad \text{if } \psi = 1$$

10 It is now easy to spot the critical role of the relative values of  $\eta$  and  $\sigma$  in shaping the economy's response to  $z$  shocks.  
11 If  $\eta = 1/\sigma$ , a parameterization that is not too unrealistic in our model,  $\phi = 0$  : the natural interest rate does not move  
12 at all with the  $z$  shock. Likewise, (13) reveals that the output gap and domestic inflation do not move either. The  
13 assumed PPI Taylor rule then prescribes that the nominal interest rate does not change.

14 The terms of trade and the real exchange rate do change and, notably, in opposite directions. The terms of trade  
15 depreciate in proportion to  $z$ , as can be readily inferred from (11) and the fact that  $r^n$  does not react to  $z$  when  $\phi = 0$ .  
16 From  $\hat{x}_t = (1-\alpha)\hat{q}_t - \hat{z}_t$ , the real exchange rate appreciates by  $\alpha\hat{z}_t$ . Under perfect international risk sharing and given  
17 world consumption, domestic consumption declines *pari passu* with the real appreciation. These responses are illustrated  
18 by the dotted green line in Figure 2, which has  $\eta = 1/\sigma = 0.5$  (and other parameter values set as in subsection 5.1.  
19 below).

20 **[PLEASE INSERT FIGURE 2 HERE]**

21 Consider now the case of  $\eta > 1/\sigma$ , still maintaining complete risk sharing ( $\psi = 1$ ). Now  $\phi$  is negative and  $r_t^n$  increases  
22 with a positive  $z$  shock. All else constant, the right hand side of (10) is higher, reflecting that the real interest rate  
23 falls below the natural interest rate. This induces an increase in aggregate demand, leading to an increase in domestic  
24 inflation and the output gap, as given by (13).

25 The rationale is that domestic and imported goods are substitutes when  $\eta > 1/\sigma$ . Hence demand for home goods  
26 at unchanged relative prices increases with higher imported food prices. Under PPI inflation targeting, the nominal  
27 interest rate must go up and, since  $\phi_\pi > 1$  (as required by the Taylor Principle), the real interest rate also rises. This in  
28 turn dampens output and home inflation. The gradual decline of  $r_t^n$  entailed by its AR(1) dynamics, coupled with the  
29 forward-looking behavior of the output gap and inflation implied by the Phillips curve and the dynamic IS, determine  
30 that convergence in output and home inflation to pre-shock levels is gradual.

31 Since  $r^n$  increases, (11) implies that that  $q^n$  must undershoot  $\Delta z$ , so the natural terms of trade deteriorate by less  
32 than if  $\eta = 1/\sigma$ . But the rise in the output gap and home inflation are not enough to fully offset the terms of trade  
33 deterioration on impact. Meanwhile, the real exchange rate still appreciates. So, again, the terms of trade and the real  
34 exchange rate move in opposite directions. Given full risk sharing, consumption falls by more than with  $\eta = 1/\sigma$ . These  
35 responses are depicted by the dotted lines of Figure 2. The reasoning is the opposite if  $\eta < 1/\sigma$  (bold line in Figure 2).

36 Now consider the opposite case of portfolio autarky. Then  $\psi = 0$  and the response of the natural interest rate to  $z$   
37 is given by:

$$\phi = -\frac{(\sigma-1)+\omega[\varphi(1-\eta)-\sigma(\eta-1/\sigma)]}{(\sigma-1)+\omega[\varphi(1-\eta)-\sigma(\eta-1/\sigma)]-\gamma(\varphi+\sigma)(1-\omega)/\alpha} \quad \text{if } \psi = 0$$

38 This is more complex than under perfect risk sharing, but still yields useful insights. Importantly,  $\phi$  does not become

1 zero even if  $\eta = 1/\sigma$ , as long as these elasticities are not exactly equal to one.<sup>8</sup> In particular, if  $\eta \leq 1/\sigma$  and  $\sigma > 1$ ,  
 2 and  $\gamma$  is not too large,  $\phi$  becomes strictly negative; this gives a strictly positive response of output and home inflation  
 3 to the shock even when  $\eta = 1/\sigma$ . Further, the lower  $\eta$ , the stronger the response. This is illustrated in Figure 3.

4 **[PLEASE INSERT FIGURE 3 HERE]**

5 The intuition is that, under significant frictions to international risk sharing, lower substitutability between the  
 6 domestic and foreign goods implies that, in response to a positive  $z_t$  shock, domestic agents must produce and export  
 7 more (in quantity terms) of the domestic good to maintain pre-shock consumption levels. Given that foreign demand for  
 8 the home good is not perfectly elastic, this causes a deterioration of the terms of trade, so  $q_t$  overshoots  $z_t$ , and  $y_t^n$  and  
 9  $(y_t - y_t^n)$  both rise. In contrast, with perfect risk sharing, the economy receives an insurance payment from abroad in  
 10 response to the shock. This payment is intended to stabilize the marginal utility of domestic consumption and, hence, is  
 11 bigger the smaller  $\eta$ : complete financial markets effectively allow the trade balance to turn negative as the world terms  
 12 of trade turn against the small open economy – and sharply so if  $\eta$  is very small.<sup>9</sup> As domestic demand for the home  
 13 good is stabilized, its supply in world markets does not increase by as much, shoring up the world price of home exports  
 14 and thus preventing further terms of trade deterioration.

15 A comparison between Figures 2 and 3 reveals that consumption drops by more than under perfect risk sharing. The  
 16 sharper drop in consumption and the rise in output then imply that the fall in the ratio of consumption to labor effort  
 17 and of welfare are also steeper.

18 Also in contrast with the perfect risk sharing case, the terms of trade and the real exchange rate can now display  
 19 some positive covariance when  $\eta < 1$ . This follows from the fact that  $\hat{x}_t = (1 - \alpha)\hat{q}_t - \hat{z}_t$  to first order, and that the  
 20 terms of trade response to  $\hat{z}$  is larger than under perfect risk sharing. This reemphasizes that the model can deliver  
 21 various covariance patterns between those two variables, depending on parameterization. Finally, with less than perfect  
 22 risk sharing, the export elasticity parameter  $\gamma$  is also important for the magnitude and sign of the responses of output  
 23 and inflation to the  $z_t$  shock.

#### 24 4. Welfare and Policy Trade-Offs

25 Our model economy is not completely "small", since it produces a differentiated good facing a downward sloping  
 26 world demand. Nominal rigidities imply that monetary policy can affect the price of the home aggregate in terms of  
 27 world consumption. Hence policy choices must take into account not only the domestic distortions caused by inflation  
 28 but also international relative price effects (known as *terms of trade externalities*), as known since Corsetti and Pesenti  
 29 (2001).

30 This section discusses how this trade-off plays out in our model. Following Faia and Monacelli (2008), the first  
 31 subsection compares the solution of the social planner's or *Ramsey* problem against the *natural* allocations that would  
 32 emerge in a flexible price competitive equilibrium (and hence PPI targeting). The second subsection follows Benigno and  
 33 Woodford (2006) and Benigno and Benigno (2006) in deriving a purely quadratic approximation of the representative  
 34 agent's welfare. The latter can then be exploited to characterize optimal policy as a targeting rule involving inflation  
 35 and output.

##### 36 4.1. The Ramsey Solution versus the Natural Outcome

37 The market clearing condition for home goods, (7), can be written as:

$$\begin{aligned} Y_t &= A_t N_t = (1 - \alpha) (P_{ht}/P_t)^{-\eta} [C_t + \varpi \Phi(C_t, (P_{ht}/P_t) Y_t)] + \varkappa X_t^\gamma (P_{ht}/P_t)^{-\gamma} C_t^* \\ &\equiv \Theta(Y_t, C_t, (P_{ht}/P_t), X_t) \end{aligned} \quad (14)$$

38 since  $H_t = (P_{ht}/P_t) Y_t$ . Equation (14) must hold at all times and is a key constraint for the planner's choices of  
 39 consumption, leisure, and the real exchange rate.

Another key constraint is the international risk sharing equation (3), which amounts to

$$C_t^\sigma [1 + \varpi \Phi(C_t, H_t)] = \kappa X_t (C_t^*)^\sigma \quad (15)$$

<sup>8</sup>This is consistent with our earlier discussion in that risk sharing imperfections become irrelevant in this model if elasticities are unitary, up to first order. That remains true up to second order under an appropriate the tax subsidy that balances out the monopolistic competition and the terms of trade externality distortions in steady state.

<sup>9</sup>The trade balance dynamics is not plotted to save on space and preserve the readability of the figures but is available from the working paper version.



1 Finally, recall that (6) gives  $P_{ht}/P_t$ , the real price of home output, a function of the real exchange rate and the food  
 2 price shock, say  $g(X_t, Z_t)$ . Given this, the Ramsey problem is then to maximize  $u(C_t) - v(N_t)$  subject to (14) and (15).  
 3 Remarkably, the Ramsey problem is static: it has the same form at each date, in each state. The Technical Appendix  
 4 shows that the Ramsey optimality condition can be written as:

$$\frac{C_t u'(C_t)}{N_t v'(N_t)} = \frac{\sigma + s_t \epsilon_{C_t}^{\Phi_C} + \vartheta_t \epsilon_{C_t}^{\Theta}}{\vartheta_t [1 - \epsilon_{Y_t}^{\Theta}] - s_t \epsilon_{H_t}^{\Phi_C}} \quad (16)$$

5 where  $s_t = \varpi \Phi_{C_t} / (1 + \varpi \Phi_{C_t})$  and  $\vartheta_t = \left(1 - s_t \epsilon_{H_t}^{\Phi_C} \cdot \epsilon_{X_t}^g\right) / (\epsilon_{X_t}^{\Theta} + \epsilon_{p_{ht}}^{\Theta} \cdot \epsilon_{X_t}^g)$ , with  $\epsilon_{X_t}^{\Theta}$  denoting the partial elasticity of  
 6  $\Theta_t$  with respect to  $X_t$ ,  $\epsilon_{p_{ht}}^{\Theta}$  the partial elasticity of  $\Theta_t$  with respect to  $P_{ht}/P_t$ , etc.<sup>10</sup>

To interpret the preceding expression, consider the perfect risk sharing case:  $\varpi = 0$ . Then the optimality condition  
 reduces to:

$$C_t u'(C_t) = N_t v'(N_t) \{ [\epsilon_{X_t}^{\Theta} + \epsilon_{p_{ht}}^{\Theta} \cdot \epsilon_{X_t}^g] \sigma + \epsilon_{C_t}^{\Theta} \}$$

7 This just says that the Ramsey planner equates the utility benefit of a one percent increase in consumption (the LHS  
 8 of the preceding equation) to its cost in terms of increased labor effort (the RHS). To understand the latter, notice that  
 9 a one percent increase in consumption increases directly the demand for home output by  $\epsilon_{C_t}^{\Theta}$ . But perfect risk sharing  
 10 requires that a one percent increase in consumption be coupled with a real depreciation of  $\sigma$  percent. This, in turn, is  
 11 associated with an increase in demand of  $[\epsilon_{X_t}^{\Theta} + \epsilon_{p_{ht}}^{\Theta} \cdot \epsilon_{X_t}^g] \sigma$  percent.

12 If  $\varpi > 0$ , the intuition remains the same, except that, if there is to be a one percent increase in consumption, the  
 13 risk sharing condition (15) can now be satisfied by changing output instead of the exchange rate. The planner then  
 14 chooses an optimal mix of output and exchange rate adjustment, taking into account the impact on world demand and  
 15 labor effort. This accounts for the extra terms in the optimality condition.

16 The Ramsey allocation is then given by (14), (15), and (16). This system depends on exogenous shocks, so the  
 17 Ramsey solution  $(C_t, N_t, X_t)$  is stochastic and generally time varying. In particular, the different elasticities in the  
 18 RHS of the optimality condition (16) are generally time varying and, more crucially, summarize the role of the different  
 19 elasticities of demand and substitution in the model. These elasticities, in fact, determine the incentives for the planner  
 20 to exploit the "terms of trade externality". To see this in the case of perfect risk sharing, note that in that case a one  
 21 percent depreciation always increases consumption by  $1/\sigma$  percent, but the size of the associated increase in labor effort,  
 22 with the resulting cost, is smaller or larger depending on  $[\epsilon_{X_t}^{\Theta} + \epsilon_{p_{ht}}^{\Theta} \cdot \epsilon_{X_t}^g]$ . This implies, *a fortiori*, that the relative  
 23 desirability of different policy rules will depend on the interplay between elasticities and how much each rule attempts  
 24 to exploit the terms of trade externality.

Our characterization of the Ramsey solution is most useful to evaluate the optimality of the *natural* allocation, and  
 hence of perfect PPI stabilization. In any flexible price market equilibrium, prices are set as a markup over marginal  
 cost,  $P_{ht} = \mu MC_t = \mu(1 - v)W_t/A_t = \mu(1 - v)(W_t/P_t)/g(X_t, Z_t)A_t$ . And since  $W_t/P_t = v'(N_t)/u'(C_t)$  we get:

$$\frac{C_t u'(C_t)}{N_t v'(N_t)} = \frac{\mu(1 - v)C_t}{g(X_t, Z_t)A_t N_t} \quad (17)$$

25 The natural allocation is therefore pinned down by (14), (15), and (17). Hence the Ramsey allocation and the natural  
 26 allocation will, in general, differ because (and only because) the Ramsey optimality condition (16) and the markup  
 27 condition (17) are not the same. The basic difference is, in fact, the terms of trade externality: the Ramsey planner  
 28 takes into account the impact of its policies on the real exchange rate, while the natural allocation ignores that impact.  
 29 To see this, assume that  $\mu(1 - v) = 1$ . Then the preceding expression for the natural allocation reduces to  $v'(N_t) =$   
 30  $u'(C_t)A_t g(X_t, Z_t)$ , which is easily seen to be the optimal labor choice condition for a planner that takes the relative  
 31 price  $g(X_t, Z_t) = P_{ht}/P_t$  as given.

32 Hence the optimality of PPI, a mainstay of the literature, hinges on how far apart the Ramsey and natural allocations  
 33 can be. Again, this will depend on the parameters underlying the different elasticities in (16) and (17). This perspective  
 34 clarifies many of the results in the literature. For example, under perfect risk sharing, if  $\eta = \gamma = 1/\sigma$ , (16) and (17)  
 35 coincide exactly provided that  $\mu(1 - v) = 1 + \varkappa/(1 - \alpha)$ . Under the additional assumption  $\alpha = \varkappa$ , this is Gali and  
 36 Monacelli's (2005) condition for PPI stabilization to be optimal. Clearly, however, this is a very special case.

<sup>10</sup>Explicit expressions for the elasticities are given in the Technical Appendix.

1 4.2. *Optimal Feasible Outcomes*

2 A Ramsey planner is constrained only by the market clearing condition (14) and the risk sharing condition (15).  
 3 The Ramsey solution, therefore, may not be available to a central bank that must also take nominal rigidities as given.  
 4 In other words, optimal feasible allocations are constrained also by the Calvo pricing equations.

5 To tackle this problem, we derive a quadratic approximation to the representative household's utility function and  
 6 then maximize the resulting objective subject to the linearized equilibrium equations described in Table 1. As discussed  
 7 in Woodford (2003), for that procedure to be correct the quadratic approximation to utility must contain no linear  
 8 terms. This can be achieved by deriving a second order approximation to some structural equations of the model, and  
 9 using them to eliminate any linear term in the second order approximation to utility.

In our model, the Technical Appendix adapts the techniques of Benigno and Woodford (2006) and Benigno and Benigno (2006) to derive a second order approximation to the utility of the representative agent of the form

$$-E \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{2} v_t' L_v v_t + v_t' L_e e_t + \frac{1}{2} l_\pi \pi_{ht}^2 \right]$$

plus a term independent of policy, where  $v_t = (\hat{y}_t, \hat{c}_t, \hat{p}_{ht}, \hat{x}_t)'$  is a vector of endogenous variables,  $e_t = (\hat{a}_t, \hat{c}_t^*, \hat{z}_t^*)'$  is the vector of shocks,  $L_v$  and  $L_e$  are matrices, and  $l_\pi$  is a scalar. The entries of  $L_v$ ,  $L_e$  and the value of  $l_\pi$  are functions of the underlying parameters of the model. The optimal policy problem is then to maximize the previous objective subject to the linearized equations given in Table 1. One can gain further insight, however, by recognizing that one can use three of the linearized equations to express the vector  $v_t$  in terms of only one of its components and the vector of shocks. In particular, the linearized equations imply that  $v_t$  can be written as

$$v_t = N \hat{y}_t + N_e e_t \tag{18}$$

for some straightforward matrices  $N$  and  $N_e$ . Inserting in the utility function, rearranging, and ignoring terms independent of policy, the objective can then be rewritten as:

$$-E \sum_{t=0}^{\infty} \beta^t \left[ \frac{1}{2} l_y (\hat{y}_t - \tilde{e}_t)^2 + \frac{1}{2} l_\pi \pi_{ht}^2 \right] \tag{19}$$

10 :where  $l_y = N' L_v N$  is a scalar and  $\tilde{e}_t = -(1/l_y) (N' L_v N_e + N' L_e) e_t$  is a linear combination of shocks.  $\tilde{e}_t$  can then  
 11 be seen as an appropriate *output target*. The weights  $l_y$  and  $l_\pi$  measure the appropriate tradeoff between inflation and  
 12 output stabilization.

The relevant constraint for the policy problem is then obtained by inserting the previous representation of  $v_t$  into the linearized New Keynesian Phillips Curve to obtain

$$\pi_{ht} = \lambda_y \hat{y}_t + \lambda_e e_t + \beta E_t \pi_{ht+1} \tag{20}$$

13 where  $\lambda_y$  and  $\lambda_e$  are functions of the parameters of the model, as described in the Technical Appendix.

14 In order to define optimal policy, we need to take a stand about the commitment possibilities open to the central  
 15 bank in order to deal with the possibility of time inconsistency. We focus on the optimal policy under the "timeless  
 16 perspective" advocated by Woodford (2003). This reduces, in our problem, to the maximization of (19) subject to (20),  
 17 taking  $\pi_0$  as given (which is a form of limited commitment).<sup>11</sup>

The resulting first order condition for optimality can be written as:

$$\pi_{ht} + \mathcal{W}_y (\Delta \hat{y}_t - \Delta \tilde{e}_t) = 0 \tag{21}$$

18 where  $\mathcal{W}_y = l_y / \lambda_y l_\pi$  is the weight on the output term and  $\Delta$  is the difference operator. This can be interpreted as a  
 19 version of "flexible inflation targeting": it combines targeting zero inflation and the change in output around the target  
 20  $\Delta \tilde{e}_t = \tilde{e}_t - \tilde{e}_{t-1}$ .

21 This formulation shows how optimal monetary policy can be analyzed in basically the same way as in the closed  
 22 economy of, say, Benigno and Woodford (2006). The open economy aspects of the model affect the rule in at least two  
 23 ways: through the weight  $\mathcal{W}_y$  assigned to output targeting and also via the definition of the output target  $\tilde{e}_t$ .

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<sup>11</sup>See Woodford (2003) or Benigno and Woodford (2005) for a discussion of optimality from a timeless perspective. The optimal policy under the timeless perspective then depends on  $\pi_0$ , and becomes the optimal policy under commitment if  $\pi_0$  is, in turn, chosen optimally. For a full argument in a related model, see Chang (1998).

To illustrate, the upper panel of Table 2 gives the relative output weight  $\mathcal{W}_y$  under different assumptions on parameters and capital market imperfections. International financial markets are parameterized by the values of  $\psi = 1$  (perfect risk sharing) down to  $\psi = 0$  (portfolio autarky), displayed in the first column of the panel. The second column corresponds to a case in which all relevant elasticities are equal to one. In that case, emphasized by Gali and Monacelli (2005) and others,  $\mathcal{W}_y = 1/5$  regardless of the degree of international capital mobility.

[PLEASE INSERT TABLE 2 HERE]

The third column assumes unit elasticities of demand, except for  $\eta = 0.25$ . As discussed in more detail in subsection 5.1. below, this is a good assumption for items such as food, which are not easily substitutable with other goods. We see that, in that case, the emphasis on output relative to inflation in the optimal targeting rule is somewhat larger than in the unit elasticity case. In addition, the output weight increases as international capital markets become less perfect, except close to the limit case of portfolio autarky. Anticipating some of our results in the next section, this suggests that an interest rate rule that depends on output in addition to inflation will become more valuable in this case if risk sharing is less perfect.

The last column in the panel assumes not only that  $\eta = 0.25$  but also that  $\gamma = 5$ . In other words, it looks at the consequences of assuming that the price elasticity of world demand for exports is large. In this case, we see that the optimal targeting rule places much more emphasis on output than if  $\gamma = 1$ , under perfect financial markets ( $\psi = 1$ ):  $\mathcal{W}_y$  becomes almost two. In this case, the result suggest, that targeting domestic inflation may be not as desirable as targeting other variables. However, the value of  $\mathcal{W}_y$  falls substantially as  $\psi$  decreases. Under portfolio autarky, in fact, the value of  $\mathcal{W}_y$  is very close to  $1/5$ , its value in the unit elasticity case.

To illustrate the influence of food price shocks on the targeting policy, the lower panel of Table 2 displays the values of the coefficient of the food price shock  $z_t^*$  in the definition of the output target  $\tilde{e}_t$ . In the case of unit elasticities, the coefficient is always zero. This in fact confirms the results of Gali and Monacelli (2005) and Gali (2008), as it says that optimal policy does not need to react to food price shocks at all. But this is, of course, a special result. In the case of low  $\eta$ , the coefficient is negative, indicating that an increase in the world relative price of food reduces the output target. The target rule then prescribes that it is optimal for policy to respond with less domestic inflation and lower actual output. The reaction is stronger as  $\psi$  falls, moving away from perfect risk sharing.

In the case of  $\eta = 0.25$  and  $\gamma = 5$ , the coefficient of  $z_t^*$  is again negative. Its absolute value is large under perfect risk sharing, and falls quite substantially as  $\psi$  approaches zero. Under perfect risk sharing the output target is more sensitive to food price shocks if the price elasticity of the world demand for exports is larger than one, but the opposite inference can be easily drawn if risk sharing is imperfect.

Before closing this section, it is worth mentioning that the optimal targeting policy just discussed is one of many available. In particular, the vector  $v_t$  was summarized by (18) in terms of output and exogenous shocks, but we could have equally expressed  $v_t$  in terms of any of its components, say the real exchange rate or consumption. This would have led to an optimal targeting rule in terms of inflation and that other variable. In other words, the policy prescriptions discussed here are optimal but not unique.<sup>12</sup> It may be the case that alternative representations may be advantageous in terms of other grounds. For example, some may argue that an optimal target rule that includes the real exchange rate in addition to domestic inflation and output is superior in terms of intuition and transparency. That argument, however, remains to be spelled out and is beyond our paper.

## 5. Welfare Properties of Simple Rules

Besides its implications for optimal policy, as characterized in the previous section, our model is useful to examine the welfare properties of monetary policy rules often seen in practice. In this section we calibrate the model and compare the PPI Taylor rule (12), which in the context of our model amounts to the so called *core* inflation targeting rule, against three well known alternatives: a *headline* CPI-based inflation targeting rule (same as (12), but with  $\pi_t$  replacing  $\pi_{ht}$ ), a *CPI forecast* rule (with  $E_t\pi_{t+1}$  instead of  $\pi_{ht}$  in (12)), and an exchange rate peg.

### 5.1. Calibration

We calibrate the model to a quarterly frequency and assume that all shocks follow AR(1) processes. From regressions of the IMF global index of food commodity prices relative to the US WPI between 2000Q1 and 2011Q4, we set the

<sup>12</sup>This explains, in particular, the differences between our targeting discussion and that of Di Paoli (2009). Di Paoli expresses  $v_t$  in terms of output *and* the real exchange rate. This naturally leads her to conclude that it is optimal to target both variables in addition to inflation. This is correct but is not the only optimal targeting procedure.

1 standard deviation of the  $z$  shock to five percent and the AR persistence coefficient to 0.85. For productivity shocks, we  
 2 set the standard deviation at 1.2 percent and the persistence parameter at 0.7. Both are consistent with estimates for  
 3 Chile, a typical small open economy for which suitably long data series exists, and also with Gali and Monacelli's (2005)  
 4 estimates for Canada, once differences in output volatility between Chile and Canada are adjusted for. For interest rate  
 5 shocks, we set a standard deviation of 0.62 and a persistence parameter of 0.6, based on our own estimates of the Taylor  
 6 rule for Chile on 1991-2008 data.

7 The transfer cost parameter  $\varpi$  is calibrated from  $\psi = \sigma/(\sigma + \varpi)$ , so that  $\psi \in [0, 1]$ . Besides the two extremes, we  
 8 also consider  $\psi = 0.9$  which is consistent with Schulhofer-Wohl's (2011) closed economy estimates. We also explored  
 9 lower values but found that the critical range is in the interval  $[0.9, 1]$ . This suggests that even small departures from  
 10 full risk sharing can have significant implications for welfare-based policy comparisons.

11 Regarding intra-temporal elasticities, while previous studies have assumed that  $\gamma = \eta$ , there is no compelling reason  
 12 to impose the equality in a small open economy context, specially given the differences between imported goods (food)  
 13 and exported goods (manufacturing/services) that motivate our model. Hence we allow  $\gamma$  to differ from  $\eta$ . Our baseline  
 14 value of  $\gamma = 5$  is consistent with estimates for manufacturing elasticities. The labor supply parameter  $\varphi$  is set to one in  
 15 the baseline<sup>13</sup>. The ratio of home good consumption to income in steady-state ( $\omega$ ) is set to 0.66, consistent with food  
 16 expenditure shares in GDP of around thirty percent.

17 We set  $Y^* = C^* = 1$  as an obvious choice of numeraire. We set  $\varepsilon = 6$ , in line with the literature. We set  $\nu$  so that  
 18  $\varepsilon(1 - \nu)/(\varepsilon - 1) = 1 + \varkappa/(1 - \alpha)$ . As discussed in subsection 4.1, this implies that when  $\eta = 1/\sigma = \gamma$  the nonstochastic  
 19 steady state is efficient.

20 We assumed that in steady state the representative household allocates about two thirds of time to leisure, trade is  
 21 balanced, and  $A = 1$ . These assumptions imply that  $C = Y = N = 0.33$  in steady state and that all relative prices are  
 22 one. From the risk sharing condition, one can then obtain  $\kappa$ . The economy-wide market clearing equation then yields  
 23  $\varkappa$ , and the household first order condition for labor gives  $\varsigma$ .

24 The coefficients of Taylor rules are calibrated as follows. Sticking to the baseline values of  $\gamma = 5$  and  $\sigma = 2$ , we  
 25 compute discounted utility values over a grid spanning from 1.25 to 3.05 (with 0.2 increments) for the coefficient on  
 26 inflation ( $\phi_\pi$ ), and from 0 to 1.0 (with 0.125 increments) for the coefficient on the output gap ( $\phi_y$ ). This is done for  
 27 each  $\eta$  and  $\psi$  under consideration. In each case, the pair  $(\phi_\pi, \phi_y)$  that maximizes discounted utility for each rule is then  
 28 picked.

29 Finally, for the peg rule we need to specify the stochastic process for the world consumer price index. We assumed  
 30 an AR(1) with considerable persistence ( $\rho = 0.99$ ) and standard deviation of 1.3 percent, as obtained from a quarterly  
 31 regression of an unweighted average of advanced countries (G-8) producer price indices during the 1990-2008 period.<sup>14</sup>

## 32 5.2. Welfare Results

33 In order to gain intuition on the relative performance of the simple policy rules, Figure 4 plots their responses to a  
 34 food price shock. For comparison, the response associated with the optimal policy is also plotted. The figure assumes  
 35 complete financial markets and  $\eta = 1/\sigma = 0.5$ : the low value of  $\eta$  is motivated by the price elasticity of food, while  
 36 setting  $\eta = 1/\sigma$  is a natural starting point since, as discussed in Section 3.2, intra- and inter-temporal substitution  
 37 effects cancel each other out. In that case, optimal policy delivers a zero coefficient on the  $z$  component of target output  
 38 and, as can be gleaned from equations (20) and (21), this implies a zero response of output and home inflation.

39 **[PLEASE INSERT FIGURE 4 HERE]**

40 Figure 4 emphasizes that the PPI rule coincides with the optimal policy in delivering a zero response of output and  
 41 domestic inflation to the  $z$  shock. But the PPI rule also implies a larger appreciation of the real exchange rate than  
 42 optimal and, by perfect risk sharing, a suboptimally large drop in consumption.

43 The CPI rule allows for output and home inflation to react to the food price shock. However, CPI stabilization  
 44 requires, on impact, a large real appreciation and a drastic drop in output, the latter to mitigate the increase in the PPI.  
 45 The appreciation translates into a large consumption drop on impact. The intuition is that stabilizing CPI inflation in  
 46 the first period amounts to stabilizing the *level* of the CPI in that period. If the PPI were not to move, the only way  
 47 to prevent an increase in the CPI is to engineer an exchange rate appreciation. The CPI rule limits the appreciation at  
 48 the expense of letting the PPI increase some in the period of the shock.

49 Expected CPI targeting performs much better. Intuitively, targeting expected CPI inflation does not prevent an  
 50 increase in the PPI on impact, and hence does not call for a real appreciation as large and under the headline CPI rule.

<sup>13</sup>We also considered  $\varphi = 0$  and  $\varphi = 3$ , values usually found in the literature, but these choices did not alter the thrust of our results.

<sup>14</sup>Restricting estimation to the pre-2008 mitigates potential small sample biases due to the deflationary effects of the 2009-10 financial crisis but either way, our results are not critically affected by the choice of this estimation window.

As a consequence, output and domestic inflation rise on impact, but only trivially (0.08% per quarter). The benefit is a consumption response that is closest to the optimal rule relative to the other rules.

In short, in the case of Figure 4, PPI targeting replicates the optimal behavior of output and domestic inflation but delivers a larger real appreciation and consumption drop than optimal; expected CPI targeting does the opposite. Which rule delivers higher welfare will depend on the relative weights of consumption and leisure in utility. We show below, with all shocks in place, that expected CPI typically has an edge, which grows with  $\eta$ , i.e. as home goods and imports become more Edgeworth substitutable.

Figure 4 also indicates that the terms of trade and the real exchange rate co-vary negatively under the optimal policy. But we find that the covariance can be positive and, in general, depends on the policy rule.<sup>15</sup> To understand why, recall that  $\hat{x}_t = (1 - \alpha)\hat{q}_t - \hat{z}_t$  to first order. Hence the covariance is  $E\hat{x}_t\hat{q}_t = (1 - \alpha)E\hat{q}_t^2 - E\hat{q}_t\hat{z}_t$ . In the case of Figure 3,  $E\hat{q}_t\hat{z}_t$  is positive, and dominates the term  $(1 - \alpha)E\hat{q}_t^2$ . But the sizes of  $E\hat{q}_t\hat{z}_t$  and  $E\hat{q}_t^2$  clearly depend on the policy rule.

Our earlier discussion emphasized that policy analysis depends on the severity of financial frictions, as given by the degree of international risk sharing. To examine this point, Figure 5 displays impulse responses for the same case as Figure 4, except that financial autarky is assumed. The expected CPI rule now delivers a consumption response quite far away from that of the optimal policy. The optimal policy no longer entails a flat response of home output and inflation to the  $z$  shock, but rather a response in between those of the PPI rule and the expected CPI rule. This suggests that the expected CPI rule is unlikely to be superior to the PPI rule under financial autarky.

[PLEASE INSERT FIGURE 5 HERE]

For further insight, Table 3 reports first and second moments of key observables over 10,000 random shock realizations for each of the three shocks in the model (the imported price shock, the productivity shock, and the monetary policy shock). This is done across policy rules and market structures, and also by adding the exchange rate peg rule to the menu of policy options.

[PLEASE INSERT TABLE 3 HERE]

Under perfect capital mobility, the expected CPI rule gets closer than the PPI rule to the optimal policy in terms of the variance of consumption. This is consistent with Figure 4. But the expected CPI rule also displays output and home inflation variability closer to optimal than the PPI rule. This reflects that Table 3 includes all shocks, while Figure 4 focuses on the response to only food price shocks.

The table then says that expected CPI targeting should dominate PPI targeting in terms of welfare, since the latter is determined by consumption, output/employment, and home inflation variability: for all of these observables, the outcomes of the expected CPI rule are closer to optimal than PPI targeting. A similar analysis implies that expected CPI targeting dominates headline CPI targeting. Finally, an exchange rate generates home inflation variability that is closest to the optimal rule, but loses badly to the other rules on other dimensions.

Table 3 also displays the corresponding statistics for  $\psi = 0.9$  and  $\psi = 0$  (portfolio autarky). It shows that, as international risk sharing becomes less perfect, the PPI rule progressively delivers outcomes closer to the optimal policy than other rules with regard to consumption, output and home inflation, becoming most clearly dominant under financial autarky.

To round up our discussion, Figure 6 reports the welfare rankings of the different rules, and examine its sensitivity to the "food-like" low elasticity assumption, letting  $\eta$  vary from the (very) low bound of 0.25 through 5. The other elasticities are kept at their baseline values. Each line in the figure reports the welfare difference, in terms of steady state consumption, between CPI targeting, expected CPI targeting, or an exchange rate peg, respectively, and PPI targeting (a positive value means that PPI is beaten by the competing rule)<sup>16</sup>.

[PLEASE INSERT FIGURE 6 HERE]

The upper panel of Figure 6 assumes complete markets. Confirming our discussion of impulse responses and moments, expected CPI targeting dominates PPI targeting across most of the relevant values of  $\eta$ . This panel also shows that

<sup>15</sup>In particular, this is the case for CPI targeting in the first two quarters following the shock. In that case, we have found that the resulting currency appreciation, combined with home price stickiness, can raise the foreign price of the domestic composite good, compensating for the negative impact of rising import prices on the terms of trade.

<sup>16</sup>Here we follow Schmitt-Grohe and Uribe (2007) and others, and report welfare measures conditional on starting at the nonstochastic steady state. Computing welfare values amounts to a simple addition of a control variable  $V_t$  to our system of non-linear equations, where  $V_t$  evolves according to the law of motion  $V_t - \beta V_t = U(C_t, N_t)$ .

1 headline CPI targeting and the exchange rate peg dominate PPI targeting as well if  $\eta$  is above two, and that the welfare  
2 advantages grow with  $\eta$ .

3 The middle panel of Figure 6 sticks to complete market and the same parameterization as the first panel except  
4 that the  $z$  shocks are assumed to be negligible. This is for comparability with previous work and to emphasize how our  
5 policy analysis depends on the properties of imported food prices. Notably, welfare gaps become noticeably narrower,  
6 thus suggesting that the smaller welfare gaps found in previous studies is partly due to the absence of  $z$  shocks in those  
7 models. More importantly for our discussion, the middle panel of Figure 6 confirms that expected CPI targeting is now  
8 welfare-dominated by PPI targeting across the  $\eta$  spectrum; it also says, however, that both rules are dominated by the  
9 headline CPI rule and the exchange rate peg rules once the intra-temporal elasticity is sufficiently large. The latter  
10 results are consistent with the theoretical claims of Faia and Monacelli (2008) as well as calibration results in Cova and  
11 Sondergaard (2004) and Di Paoli (2009). That the CPI rule or the peg can beat the PPI rule provides some rationale  
12 for the usual central bank practice of targeting headline CPI rather than the PPI. What is new here is that expected  
13 CPI targeting, a rule that was not considered in previous studies, appears superior to all others if food price shocks are  
14 realistically volatile.

15 Finally, the lower panel of Figure 6 reinstates the full menu of shocks but assumes that risk sharing is imperfect,  
16 even if seemingly slightly so ( $\psi = 0.9$ ). The figure corroborates the results of Table 3 in restoring the welfare supremacy  
17 of PPI targeting, except again when  $\eta$  is (unrealistically for food) high. This proviso disappears, however, as  $\psi$  becomes  
18 smaller. Under portfolio autarky, PPI targeting easily beats the other rules.<sup>17</sup>

19 We have explored many other parameterizations, which we do not report to save space. The role of the size of the  
20 parameter  $\psi$  bears mentioning, however. While the analysis is starkest under the polar assumptions of perfect risk  
21 sharing and portfolio autarky, we have found that it changes quickly as  $\psi$  drops just below one. This suggests that  
22 only mild frictions to the financial technology can be quite significant, although a further examination is warranted.  
23 Finally, we have explored the roles of export price elasticity  $\gamma$ , the elasticity of labor supply ( $1/\varphi$ ), and the price-  
24 stickiness parameter  $\theta$ . Provided that the latter is kept within sensible ranges (above 0.3) so a New Keynesian setup  
25 remains meaningful, the export price elasticity  $\gamma$  has the greatest effect on welfare rankings. Yet, once risk sharing is  
26 incomplete ( $\psi \leq 0.9$ ), the dominance of flexible PPI targeting is only marginally dented for alternative calibrations of  
27 these parameters and generally becomes stronger with lower  $\gamma$ .

## 28 6. Final Remarks

29 While our analysis places fewer restrictions on the economic environment than previous studies, it by no means  
30 includes all cases of interest. It may be necessary to ask, for example, what are the implications of assuming that food  
31 can be produced at home. While this extension is beyond the scope of the present paper, our analysis suggests the  
32 resulting policy prescriptions are likely to depend on export price elasticities and degree of capital mobility, both of  
33 which can be highly country specific.

34 One obvious avenue for future research is to estimate versions of the model discussed here, which would yield lessons  
35 for real world policy formulation. In this regard, our formulation of international risk sharing should prove especially  
36 useful, because of its tractability and parsimony.

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<sup>17</sup>The corresponding figure looks very much like the lower panel of Figure 6 and is omitted here to save space.

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Table 1 : Linearized Model Equations

**Log linear versions of structural equations:**

$$\hat{c}_t = \psi \left[ \frac{1}{\sigma} \hat{x}_t + \hat{c}_t^* \right] + (1 - \psi) [\hat{p}_{ht} + \hat{y}_{ht}] \quad (\text{L1})$$

$$0 = (1 - \alpha) \hat{p}_{ht} + \alpha (\hat{x}_t + \hat{z}_t) \quad (\text{L2})$$

$$\hat{y}_{ht} = -[\eta\omega + \gamma(1 - \omega)] \hat{p}_{ht} + \omega \hat{c}_t + \gamma(1 - \omega) \hat{x}_t + (1 - \omega) \hat{c}_t^* \quad (\text{L3})$$

$$\pi_{ht} = \lambda [\sigma \hat{c}_t + \varphi \hat{y}_{ht} - \hat{p}_{ht} - (1 + \varphi) \hat{a}_t] + \beta E_t \pi_{ht+1} \quad (\text{L4})$$

where  $\psi = \frac{\sigma}{\sigma + \varpi}$  and  $\lambda = \frac{1 - \theta}{\theta} \frac{1 - \beta\theta}{1 + \varphi\varepsilon}$ .

**Flexible Price ("Natural") Variables:**

$$\hat{c}_t^n = \psi \left[ \frac{1}{\sigma} \hat{x}_t^n + \hat{c}_t^{*n} \right] + (1 - \psi) [\hat{p}_{ht}^n + \hat{y}_{ht}^n] \quad (\text{N1})$$

$$0 = (1 - \alpha) \hat{p}_{ht}^n + \alpha (\hat{x}_t^n + \hat{z}_t) \quad (\text{N2})$$

$$\hat{y}_{ht}^n = -[\eta\omega + \gamma(1 - \omega)] \hat{p}_{ht}^n + \omega \hat{c}_t^n + \gamma(1 - \omega) \hat{x}_t^n + (1 - \omega) \hat{c}_t^{*n} \quad (\text{N3})$$

$$0 = \sigma \hat{c}_t^n + \varphi \hat{y}_{ht}^n - \hat{p}_{ht}^n - (1 + \varphi) \hat{a}_t^n \quad (\text{N4})$$

**Deviations from Natural Variables ("Gaps "):**

$$\tilde{c}_t = \psi \left[ \frac{1}{\sigma} \tilde{x}_t \right] + (1 - \psi) [\tilde{p}_{ht} + \tilde{y}_{ht}] \quad (\text{G1})$$

$$0 = (1 - \alpha) \tilde{p}_{ht} + \alpha \tilde{x}_t \quad (\text{G2})$$

$$\tilde{y}_{ht} = -[\eta\omega + \gamma(1 - \omega)] \tilde{p}_{ht} + \omega \tilde{c}_t + \gamma(1 - \omega) \tilde{x}_t \quad (\text{G3})$$

$$\pi_{ht} = \lambda [\sigma \tilde{c}_t + \varphi \tilde{y}_{ht} - \tilde{p}_{ht}] + \beta E_t \pi_{ht+1} \quad (\text{G4})$$

*Note:* This table collects the linearized equations of the model.



**Table 2. Calibrated Weights in the Optimal Policy Rule**

a) Relative Weight of Output

$\psi$	Unit Elasticities	$\eta = 0.25$	$\eta = 0.25$ and $\gamma=5$
1	0.2	0.217	1.968
0.8	0.2	0.225	0.352
0.6	0.2	0.238	0.262
0.4	0.2	0.258	0.24
0.2	0.2	0.300	0.246
0	0.2	0.296	0.201

b) Relative Weight of Food Price Shock in Target Output

$\psi$	Unit Elasticities	$\eta = 0.25$	$\eta = 0.25$ and $\gamma=5$
1	0	-0.173	-0.372
0.8	0	-0.199	-0.152
0.6	0	-0.231	-0.078
0.4	0	-0.271	-0.043
0.2	0	-0.321	-0.02
0	0	-0.324	-0.022

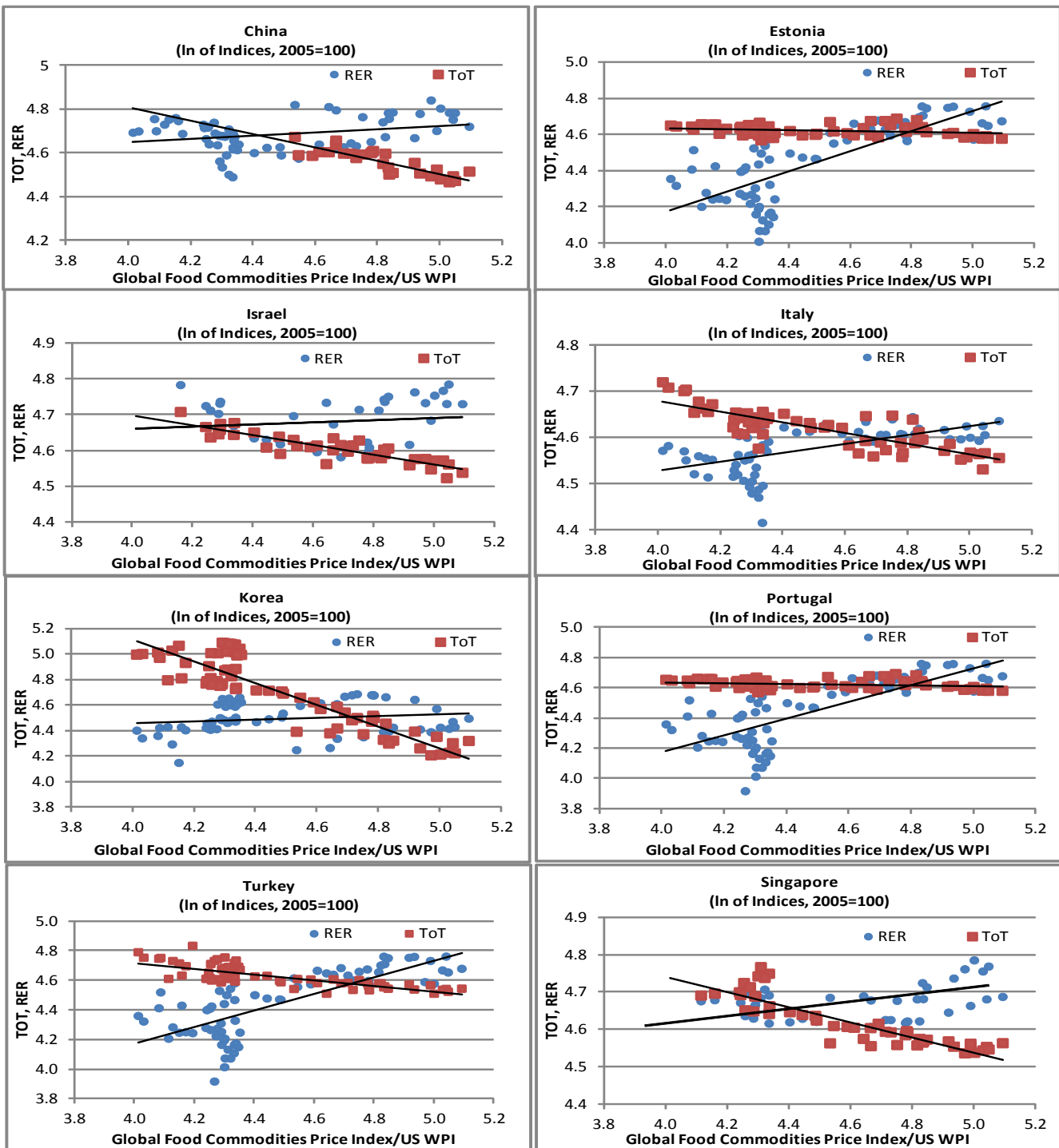
*Note:* The first panel reports the weight of output relative to inflation in an optimal policy rule. The second panel gives the weight of the food price shock in target output under the optimal policy rule.

**Table 3. Model Statistics Under Simulated Random Shocks**

	Complete Markets ( $\psi=1.0$ )					Imperfect Risk Sharing ( $\psi=0.9$ )					Financial Autarky ( $\psi=0$ )				
	Optimal Policy	PPI Rule	CPI Rule	EXP(CPI) Rule	PEG Rule	Optimal Policy	PPI Rule	CPI Rule	EXP(CPI) Rule	PEG Rule	Optimal Policy	PPI Rule	CPI Rule	EXP(CPI) Rule	PEG Rule
Standard deviations (in %)	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
Domestic Output	0.990	0.668	0.780	0.752	1.047	0.628	0.642	0.748	0.711	1.053	0.492	0.502	0.568	0.540	0.540
Consumption	0.408	0.529	0.547	0.499	0.546	0.434	0.751	0.598	0.534	0.612	0.677	0.572	0.598	0.629	1.756
Real Exchange Rate	2.475	3.206	3.315	3.021	3.310	2.353	3.112	3.219	2.948	3.256	1.985	2.504	2.493	2.429	2.764
CPI inflation	1.615	1.777	1.519	1.839	1.844	1.464	1.754	1.538	1.846	1.841	1.503	1.898	1.803	1.857	8.786
Domestic Inflation	0.361	0.234	0.129	0.152	0.473	0.279	0.049	0.136	0.144	0.486	0.007	0.091	0.290	0.301	0.713
<b>Means in % of SS deviation</b>															
Domestic Output	0.021	-0.038	0.003	0.000	-0.132	0.009	0.009	0.003	0.002	-0.131	0.007	0.006	-0.008	-0.011	-0.121
Consumption	-0.003	-0.013	-0.007	-0.008	-0.032	-0.002	-0.005	-0.007	-0.008	-0.041	0.001	-0.007	-0.022	-0.029	-0.113
Real Exchange Rate	-0.001	-0.053	-0.012	-0.027	-0.168	0.003	-0.005	-0.006	-0.007	-0.006	-0.011	-0.007	-0.013	-0.025	-0.161
CPI inflation	0.012	0.001	0.073	0.038	0.017	0.010	0.025	0.083	0.044	0.017	0.011	0.025	0.083	0.044	0.017
Domestic Inflation	0.000	-0.015	0.061	0.022	0.001	0.000	0.009	0.071	0.027	0.001	0.000	0.002	0.153	0.173	0.003

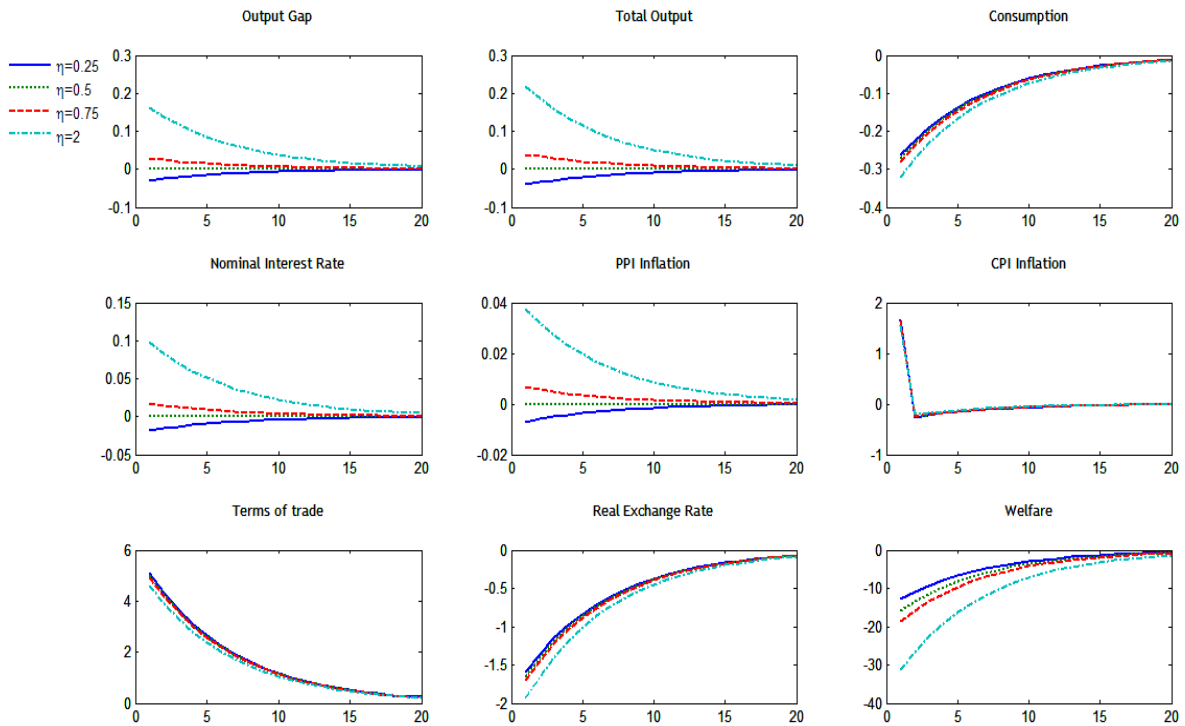
*Note:* This table reports standard deviations and mean deviations from non-stochastic steady state for main aggregates. They are computed from simulating 10,000 random shocks to the processes for import food price index, home productivity, and monetary policy, for the case  $\eta=1/\sigma=0.5$ ,  $\gamma=5$ , and baseline values for the other parameters. Results are displayed for optimal monetary policy, PPI inflation targeting (IT), *headline* CPI IT, *expected* CPI IT, and an exchange rate peg. The three panels correspond to perfect risk sharing, imperfect risk sharing, and financial autarky.

**Figure 1. Covariance of the Terms of Trade and Real Exchange Rate with World Food Prices**



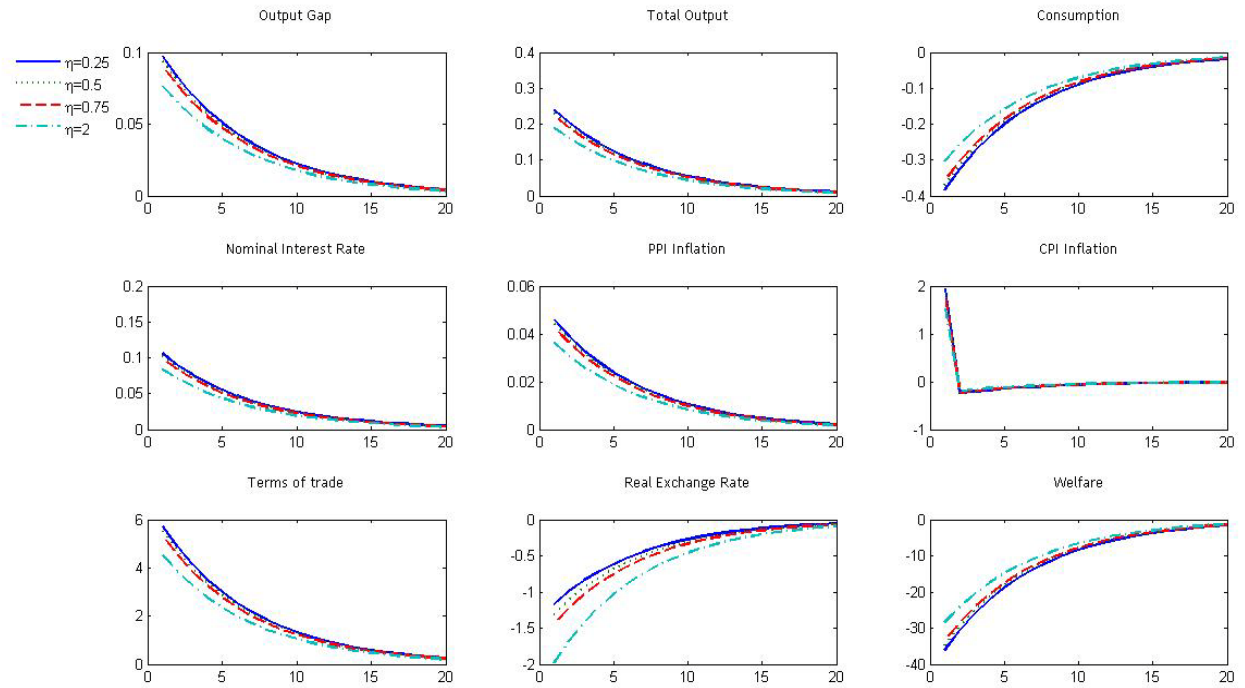
*Note:* This figure plots the natural logarithm of the terms of trade and real effective exchange rate indices for each country (both normalized so that 2005=100), against the natural logarithm of the IMF index of world food commodity prices deflated by the US Wholesale Price Index (also normalized so that 2005=100) for the period of 1994:Q1 to 2011:Q4.

**Figure 2. Impulse-responses to a world food price shock under full risk sharing**



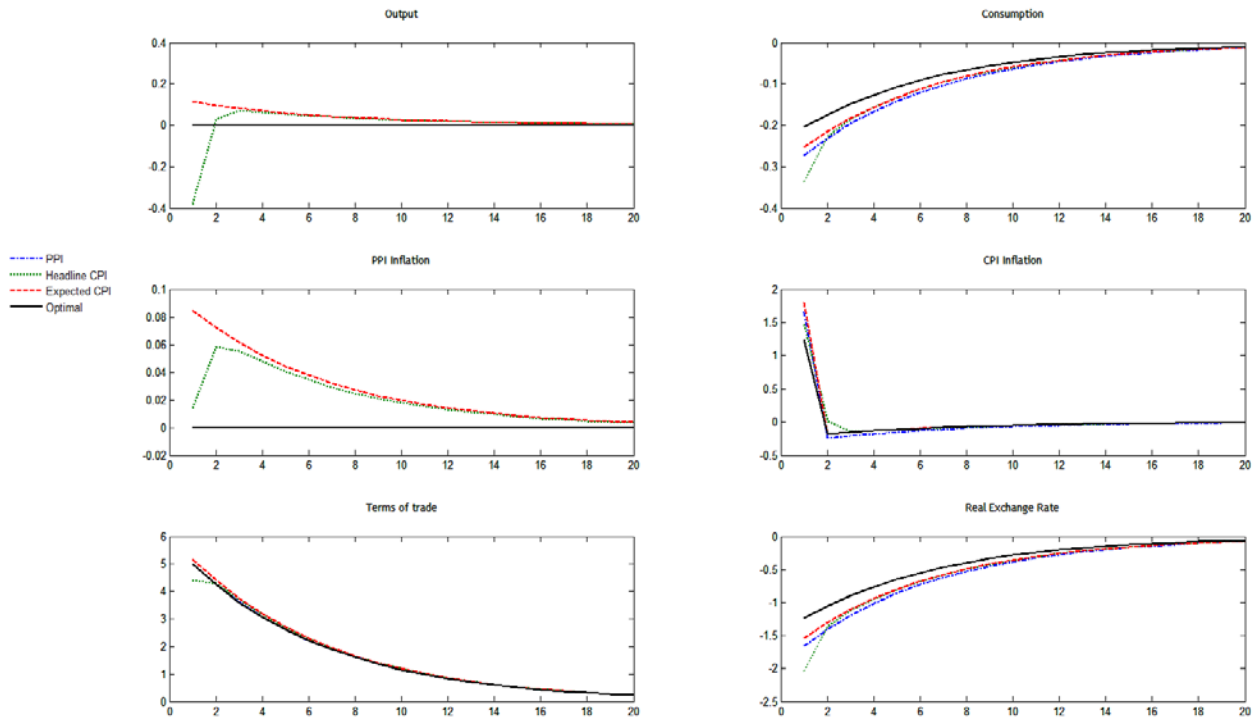
*Note:* This figure plots the responses (in percentage points) of the main aggregates of the model to a one standard deviation shock (5 percent) to the imported food price index under perfect international risk sharing ( $\psi=1$ ). A flexible PPI Taylor rule is assumed. The inter-temporal substitution elasticity ( $\sigma$ ) is equal to 2. The remaining parameters are set to the baseline values discussed in section 5.1 of the main text.

**Figure 3. Impulse-responses to a world food price shock under financial autarky**



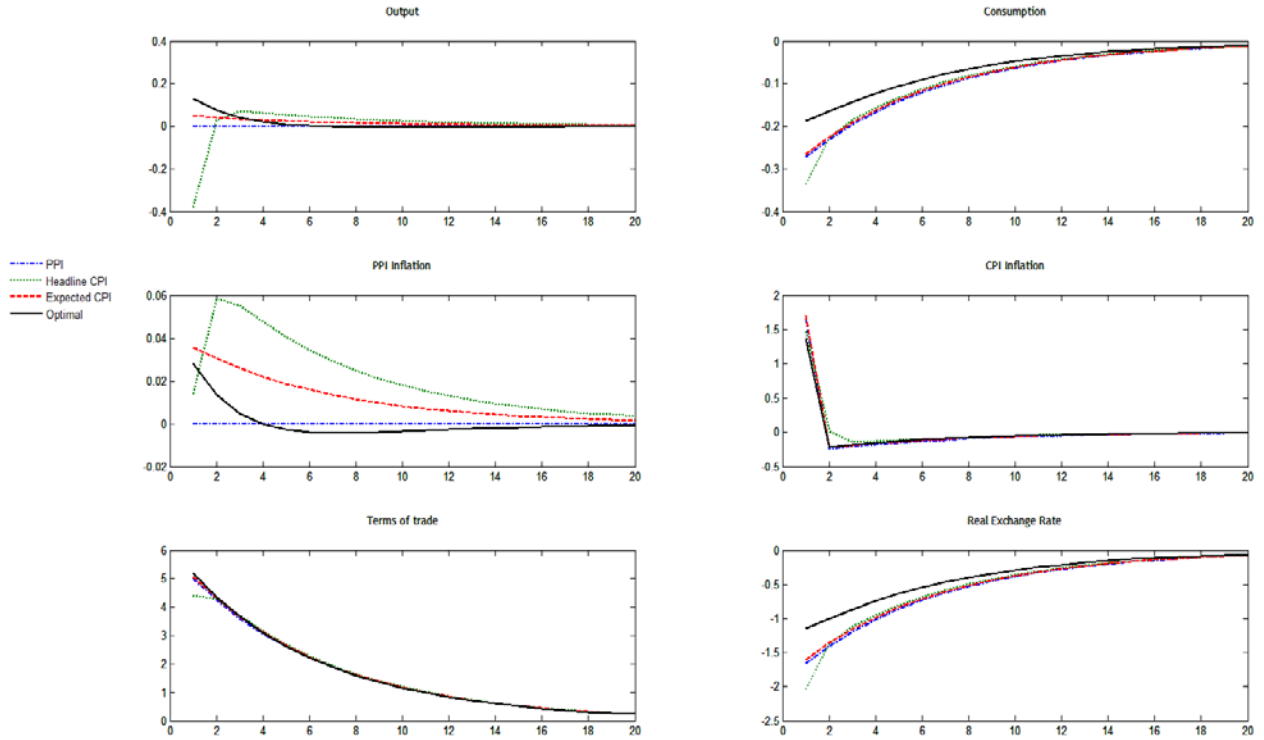
*Note:* This figure plots the responses (in percentage points) of the main aggregates of the model to a one standard deviation shock (5 percent) to the imported food price index under financial autarky ( $\psi=0$ ). A flexible PPI Taylor rule is assumed. The inter-temporal elasticity ( $\sigma$ ) is equal to 2. The remaining parameters are at baseline values.

**Figure 4: Optimal Policy vs. Simple IT Rules under Complete Markets: IRs to  $z^*$  shock**



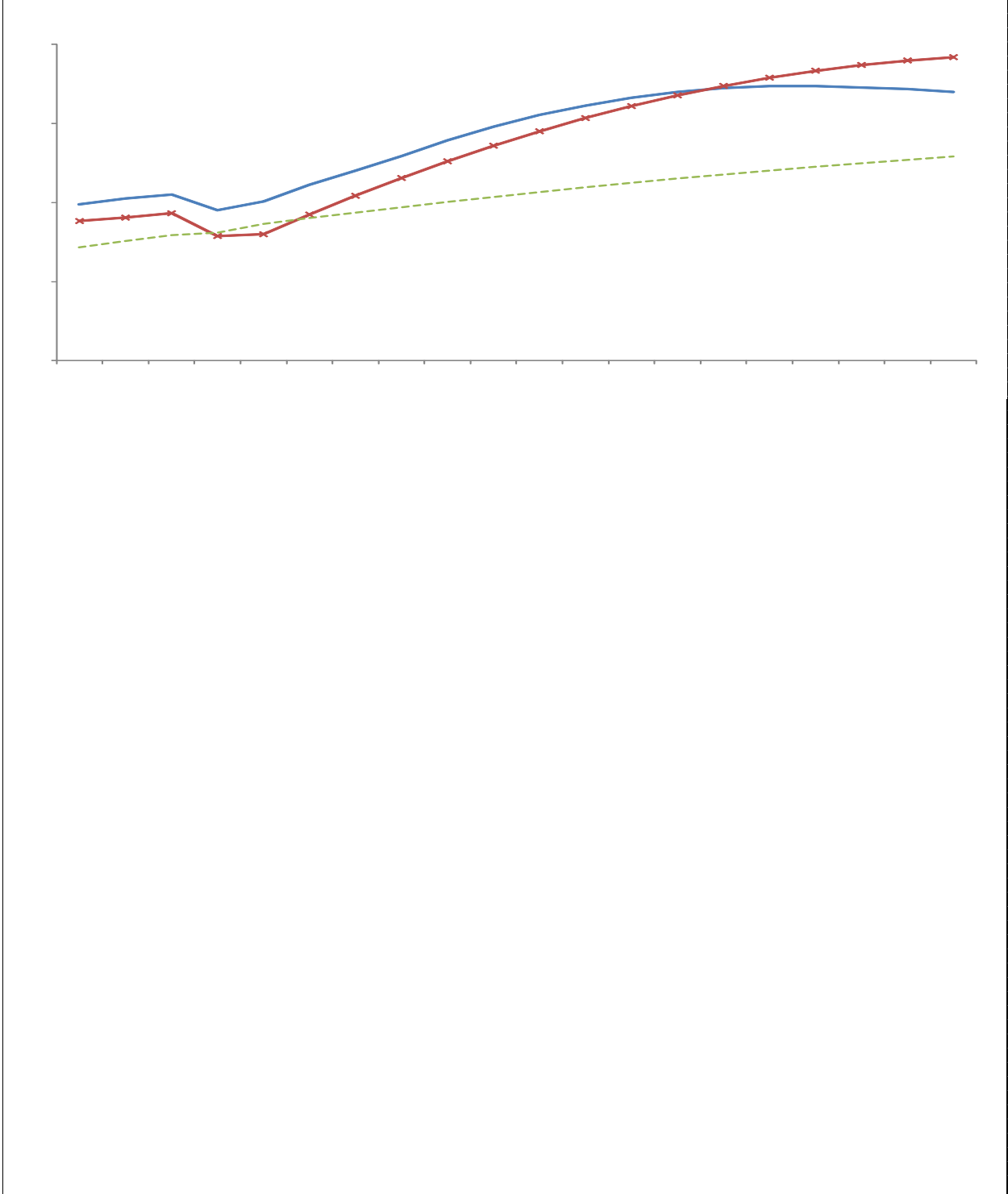
*Note:* This figure plots the responses (in percentage points) of the main aggregates of the model to a one standard deviation shock (5 percent) to the imported (food) price index under perfect international risk sharing ( $\psi=1$ ). It is assumed that  $\eta=1/\sigma=0.5$ ,  $\gamma=5$ , and that other parameters are kept at baseline values.

**Figure 5: Optimal Policy vs. Simple IT Rules under Financial Autarky: IRs to  $z^*$  shock**



*Note:* This figure plots the responses (in percentage points) of main model aggregates to a one standard deviation shock (5 percent) to the imported food price index under financial autarky ( $\psi=0$ ). It is assumed that  $\eta=1/\sigma=0.5$  and  $\gamma=5$ , and that other parameters are kept at baseline values.

Figure 6: Welfare Differences Across Simple Policy Rules



*Note:* This figure plots differences in conditional welfare, expressed as percent of non-stochastic steady state consumption, between pairs of competing policy rules for alternative values of  $\eta$ . The upper panel assumes perfect risk sharing ( $\psi=1$ ) and all shocks present. The middle panel assumes perfect risk sharing but  $z^*$  shocks are set to zero. The lower panel assumes all shocks are present but international risk sharing is imperfect ( $\psi=0.9$ ).